

8. a) Write  $26^{\frac{2}{5}}$  in radical form in 2 ways.

$$\sqrt[5]{26^2} \quad \text{OR} \quad (\sqrt[5]{26})^2$$

b) Write  $\sqrt{6^3}$  and  $(\sqrt[4]{19})^3$  in exponent form.

$$6^{\frac{3}{2}} \quad 19^{\frac{3}{4}}$$

9. Evaluate.

a)  $(-27)^{\frac{4}{3}}$

$$(\sqrt[3]{-27})^4$$

$$(-3)^4 = 81$$

b)  $0.01^{\frac{3}{2}}$

$$(\sqrt{0.01})^3$$

$$= (0.1)^3$$

$$= 0.001$$

c)  $81^{\frac{3}{4}}$

$$(\sqrt[4]{81})^3$$

$$= 3^3$$

$$= 27$$

10. Evaluate each power.

a)  $7^{-2} = \frac{1}{7^2}$

$$\frac{1}{49}$$

b)  $(\frac{10}{3})^{-3}$

$$= (\frac{3}{10})^3$$

$$= \frac{27}{1000}$$

11. Evaluate each power.

a)  $16^{-\frac{5}{4}}$

$$(\frac{1}{16})^{\frac{5}{4}}$$

$$(\sqrt[4]{\frac{1}{16}})^5$$

$$= (\frac{1}{2})^5 = \frac{1}{32}$$

b)  $(\frac{25}{36})^{-\frac{1}{2}}$

$$(\frac{36}{25})^{\frac{1}{2}}$$

$$\sqrt{\frac{36}{25}}$$

$$= \frac{6}{5}$$

**CHALLENGE – A-Level Questions**

12. Simplify. Explain your reasoning.

a)  $(25a^4b^2)^{\frac{3}{2}}$

$$\sqrt{25a^4b^2}$$

$$(5a^2b)^3$$

$$= 125a^6b^3$$

b)  $(x^3y^{-\frac{3}{2}})(x^{-1}y^{\frac{1}{2}})$

~~$$x^3y^{-\frac{3}{2}}$$~~

$$x^{3+(-1)}y^{-\frac{3}{2}+\frac{1}{2}}$$

$$= x^2y^{-\frac{2}{2}}$$

$$= \frac{x^2}{y^1}$$

Chapter 4 Questions to help you study for your assessment

Please do these questions without your calculator but you may use your Perfect Squares/Cubes sheet.

1. Simplify by writing as a single power. Show your reasoning.

a)  $(5a^5)^2 = 25a^{10}$       b)  $0.8^2 \cdot 0.8^{-7} = 0.8^{2+(-7)} = 0.8^{-5}$       c)  $\left[ \left(-\frac{4}{5}\right)^2 \right]^{-3} \div \left[ \left(-\frac{4}{5}\right)^4 \right]^{-5} = \left(-\frac{4}{5}\right)^{-6} \div \left(-\frac{4}{5}\right)^{-20} = \left(-\frac{4}{5}\right)^{-6-(-20)} = \left(-\frac{4}{5}\right)^{14}$

2. Simplify. Show your reasoning.

a)  $m^4 n^{-2} \cdot m^2 n^3 = m^6 n^1$       b)  $\frac{36x^4 y^3}{24x^{-2} y} = \frac{3x^6 y^2}{2}$       c)  $a^{\frac{1}{5}} \times a^{\frac{1}{5}} = a^{\frac{2}{5}}$

3. Tell whether each number is rational or irrational. Explain how you know.

a)  $\sqrt{\frac{49}{16}}$  rational both numerator and denominator are square numbers, so can be written as a fraction.  
 b)  $\sqrt[3]{-30}$  irrational, -30 is not a perfect cube number.  
 c) 1.21 rational, 1.21 is a terminating decimal number.

4. Simplify each radical.

a)  $\sqrt{63} = 3\sqrt{7}$  (tree diagram: 63, 7, 9, 3x3)  
 b)  $\sqrt[3]{108} = 3\sqrt[3]{4}$  (tree diagram: 108, 2, 54, 6, 9, 2x3, 3x3)  
 c)  $\sqrt[4]{128} = 2\sqrt[4]{8}$  (tree diagram: 128, 2, 64, 8, 2x2x2x2)

5. Write each radical in simplest form, if possible.

a)  $\sqrt{30}$  not possible, 30 does not have any factors which are square numbers.  
 b)  $\sqrt[3]{32} = 2\sqrt[3]{4}$  (tree diagram: 32, 2, 16, 2x8, cube number)  
 c)  $\sqrt[4]{48} = 2\sqrt[4]{3}$  (tree diagram: 48, 3, 16, 2, 8, 2x4, 2x2)

6. Write each mixed radical as an entire radical.

a)  $7\sqrt{3} = \sqrt{49 \times 3} = \sqrt{147}$   
 b)  $2\sqrt[3]{4} = \sqrt[3]{8 \times 4} = \sqrt[3]{32}$   
 c)  $2\sqrt[5]{3} = \sqrt[5]{32 \times 3} = \sqrt[5]{96}$  (with  $2^5$  written next to the radical)

7. Evaluate each power.

a)  $1000^{\frac{1}{3}} = \sqrt[3]{1000} = 10$   
 b)  $0.25^{\frac{1}{2}} = \sqrt{0.25} = 0.5$   
 c)  $(-8)^{\frac{1}{3}} = \sqrt[3]{-8} = -2$   
 d)  $\left(\frac{16}{81}\right)^{\frac{1}{4}} = \sqrt[4]{\frac{16}{81}} = \frac{2}{3}$